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COMBINED DIFFRACTION AND REFLECTION BY A VERTICAL WEDGE: PCDFRAC USER'S MANUAL

by

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Wedge angle

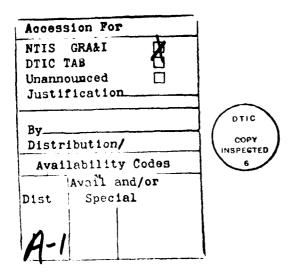
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PREFACE

The work in this report was authorized by the US Army Corps of Engineers (USACE), Coastal Engineering Functional Area of Civil Works Research and Development, under Waves at Entrances Work Unit 31673, Harbor Entrances and Coastal Channels Program, at the Coastal Engineering Research Center (CERC) of the US Army Engineer Waterways Experiment Station (WES). Messrs. John H. Lockhart, Jr., John G. Housley, James Crews, and Charles W. Hummer were USACE Technical Monitors. Dr. Charles L. Vincent is CERC Program Manager.

This report was prepared by Mr. James M. Kaihatu, Research Hydraulic Engineer, and Dr. H. S. Chen, Research Hydraulic Engineer, Coastal Oceanography Branch (CR-O), Research Division (CR), CERC. Work was performed under direct supervision of Dr. Edward F. Thompson, Chief, CR-O, and Mr. H. Lee Butler, Chief, CR, CERC. Chief and Assistant Chief, CERC, are Dr. James R. Houston and Mr. Charles C. Calhoun, Jr., respectively. This report was edited by Ms. Shirley A. J. Hanshaw, Information Products Division, Information Technology Laboratory, WES.

During publication of this report, COL Dwayne G. Lee, EN, was Commander and Director of WES. Dr. Robert W. Whalin was Technical Director.



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CONVERSION FACTORS, NON-SI TO SI (METRIC) UNITS OF MEASUREMENT

Non-SI units of measurement can be converted to SI (metric) units as follows:

Multiply	By	To Obtain
feet	0.3048	metres
feet per second squared	0.3048	metres per second squared
inches	2.54	centimetres

COMBINED DIFFRACTION AND REFLECTION BY A VERTICAL WEDGE PCDFRAC USER'S MANUAL

PART I: INTRODUCTION

Background

- 1. In coastal/ocean engineering practice it is often important to be able to determine the wave heights near such marine structures as jetties, breakwaters, platforms, and docks. Such information aids engineers in evaluating their marine structure designs, especially in the areas of energy transmissibility, sediment transport, and structural strength. Wave heights in the near field have usually been presented in the form of dimensionless wave amplification factors which are defined as the ratio of near field wave height to incident wave height.
- 2. Early studies (Wiegel 1962) presented a dimensionless graphical solution for diffraction by a semi-infinite breakwater. Subsequently, these diagrams have been incorporated into every edition of the Shore Protection Manual (SPM) (1984), and they remain useful tools for preliminary engineering design. However, the diagrams cannot account for wave reflection from the breakwater.
- 3. Chen (1987) has recently presented an analytical solution for the total wave field due to combined diffraction and reflection by a vertical wedge of arbitrary wedge angle, as well as the FORTRAN program WEDGE, which calculates the amplification factors and the phases of the waves in the near field. Solutions for 0- and 90-deg wedge angle, presented in amplification factor diagrams, are also included. WEDGE was designed to operate on a conventional mainframe computer.
- 4. The FORTRAN program PCDFRAC is a version of WEDGE which is operable on an IBM or IBM-compatible personal computer (PC). It can be used to calculate wave amplification factors due to combined diffraction and reflection near jettied harbor entrances, quay walls, and other such structures. Jetties and breakwaters can be approximated by a semi-infinite breakwater in which the wedge angle is equal to zero. Corners of docks and quay walls can be represented by setting the wedge angle equal to 90 deg. Additionally, such natural

diffracting and reflecting obstacles as rocky headlands can be approximated by setting a particular value for the wedge angle.

Objective

- 5. The problem of determining wave heights near marine structures has been recognized for some time, and it is made more complex by the combination of water wave diffraction and reflection effects present near such structures. Consequently, a method must be developed to not only solve the physical problem but also accommodate the needs of various users in a flexible and effective manner. This report addresses this problem by summarizing an analytical solution for the diffraction and reflection of monochromatic incident waves caused by a vertical wedge. It also presents PCDFRAC which calculates the analytical solution to the combined diffraction and reflection problem. The PC code makes the solution much more available to users than did the mainframe version.
 - 6. The objectives of this report are to:
 - a. Document the program PCDFRAC.
 - b. Instruct the user (Corps or non-Corps) in the proper application of the program in field situations and in the interpretation of results.
 - <u>c</u>. Instruct the user in setting up PCDFRAC in a personal computer and to run the code.
 - d. Present the user with relevant examples of program execution.

Report Organization

- 7. The report herein is organized as follows:
 - <u>a.</u> Part I introduction containing background, objectives, and program availability.
 - b. Part II brief theoretical outline of the basis of the model.
 - c. Part III details of the model, including program convention and required equipment for proper program execution.
 - <u>d.</u> Part IV procedures for installing the program onto a personal computer.
 - e. Part V program execution and usage examples.

Program Availability

8. The program PCDFRAC calculates wave heights due to diffraction and reflection by a vertical wedge of arbitrary wedge angle in constant water depth, including the zero wedge angle (semi-infinite breakwater) case. It also calculates the wavelength from the linear dispersion relation by using a Pade approximation (Chen and Thompson 1985). It can be used on an IBM or IBM-compatible personal computer and is available on 5-1/4-in.* floppy diskette in Microsoft FORTRAN 77. The diskette contains the source code PCDFRAC.FOR and the executable file PCDFRAC.EXE as well as sample input and output files. It can be obtained directly from the authors at the following address: Coastal Oceanography Branch, Research Division, Coastal Engineering Research Center, US Army Engineer Waterways Experiment Station, PO Box 631, Vicksburg, MS 39180-0631.

^{*} A table of factors for converting non-SI units of measurement to SI (metric) units is presented on page 3.

PART II: THEORETICAL BACKGROUND

9. This part of the report summarizes the linear formulation and solution of water wave diffraction and reflection by a vertical wedge of arbitrary wedge angle, with a semi-infinite breakwater considered a special case in which the wedge angle is zero. Water depth h^* is constant, the bottom is rigid and impermeable, and the monochromatic incident waves of infinitesimal amplitude come from infinity at an angle α . The cylindrical coordinate system $(r,\,\theta,\,z)$ is chosen, with z=0 representing the undisturbed free surface and the positive z-axis positioned vertically upward. The tip of the wedge is chosen to be the origin of the coordinate system, and the two rigid walls of the wedge are at $\theta=0$ and $\theta=\theta_0$, respectively, as shown in Figure 1. Cartesian coordinates $(x,\,y,\,z)$, corresponding to the cylindrical coordinates, are also used on occasion and are shown in the same figure. The wedge angle is thus defined as $2\pi-\theta_0$, while the water domain is defined as $0 \le \theta \le \theta_0$ and $0 \ge z \ge -h$.

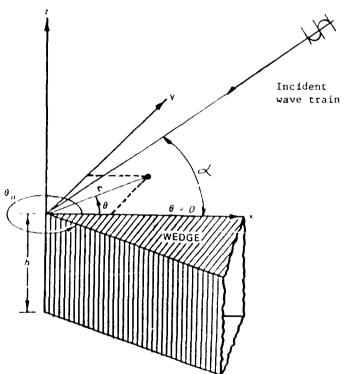


Figure 1. A vertical wedge of arbitrary angle

^{*} For convenience, symbols and abbreviations are listed in the Notation (Appendix C).

10. For the problem at hand, the velocity field for wave motion in an ideal fluid may be represented by the velocity potential $\phi(r,\theta,z,t)$ and is expressed as follows:

$$\phi(r,\theta,z,t) = A_0 \frac{\cosh k(z+h)}{\cosh kh} \phi(r,\theta)e^{i\omega t}$$
 (1)

where

$$A_{o} = -iga_{o}/\omega$$

$$i = \sqrt{-1}$$

g = gravitational acceleration

 $a_0 = incident wave amplitude$

 ω = radian frequency

k = wave number

 $\phi(r,\theta)$ = velocity potential function in the horizontal plane

t = time variable

The wave number k must be real and satisfy the following linear dispersion relation:

$$\omega^2 = gk \tanh kh$$
 (2)

ll. Several properties of wave mechanics are dependent on the velocity potential component $\phi(r,\theta)$. For example, the free surface elevation in may be expressed in terms of $\phi(r,\theta)$ as follows:

$$\eta = a_{o} \phi(r,\theta) e^{i\omega t}$$
 (3)

The flow velocity u is also dependent on $\phi(\mathbf{r},\delta)$. This quantity is important in the area of sediment transport and may be expressed in polar coordinates as follows:

$$u_{r} = \frac{\partial \Phi}{\partial r} = \Lambda_{o} \frac{\cosh k(z+h)}{\cosh kh} \frac{\partial \Phi}{\partial r} e^{i\omega t}$$
 (4)

$$u_{\theta} = \frac{1}{r} = \frac{\partial \Phi}{\partial \theta} = A_0 \frac{\cosh k(z+h)}{\cosh kh} \frac{1}{r} \frac{\partial \Phi}{\partial r} e^{i\omega t}$$
 (5)

12. For an incident plane wave train coming from the α direction (as shown in Figure 1) where the free surface elevation of the incident wave may be described by:

$$\eta_{i} = a_{0} e^{i(kr \cos \alpha + \omega t)}$$
(6)

the analytical solution for a wave field by a vertical wedge of arbitrary wedge angle (based on the linearized wave theory) may be written as follows (Chen 1987):

$$\varphi(\mathbf{r},\theta) = \frac{2}{\nu} \left[J_{o}(\mathbf{k}\mathbf{r}) + 2 \sum_{n=1}^{\infty} e^{i\mathbf{n}\pi/2\nu} J_{n/\nu} \cos \frac{n\alpha}{\nu} \cos \frac{n\theta}{\nu} \right]$$
 (7)

where

$$v = \frac{\theta_0}{\rho} / \pi$$
 (8)

$$J_0 = \text{zeroth order Bessel function of the first kind}$$

$$J_{n/v} = n/v \quad \text{order Bessel function of the first kind}$$

The semi-infinite breakwater is a special case of the diffraction and reflection problem where the wedge angle is equal to zero and $\nu=2$. The solution of Equation 1 for this case is

$$\phi(\mathbf{r},\theta) = J_0(\mathbf{k}\mathbf{r}) + 2\sum_{n=1}^{\infty} e^{in\pi/4} \frac{Jn}{2} \cos \frac{n\alpha}{2} \cos \frac{n\theta}{2}$$
 (9)

The velocity potential function $\phi(r,\theta)$ in Equations 7 and 9 is a complex function and may be expressed as

$$\phi = |\phi| e^{i\beta} \tag{10}$$

where

$$|\phi| = \left[\operatorname{Im}(\dot{\gamma})\right]^2 + \left[\operatorname{Re}(\phi)\right]^2 = \text{amplitude of } \phi$$
 (11)

$$\beta = \tan^{-1} \left[\frac{Im(\phi)}{Re(\phi)} \right] = \text{phase of } \phi$$
 (12)

and where

Im ϕ = imaginary part of ϕ

Re ϕ = real part of ϕ

Substituting Equation 10 into Equation 3, the following is obtained:

$$n = a_0 |\phi| e^{i(\beta + \omega t)}$$
 (13)

This expression represents the actual water surface elevation at a point in the water domain bounded by a vertical wedge of arbitrary wedge angle. Since the incident wave train is expressed in Equation 6, the normalized water surface elevation in the near field may be expressed as

$$\frac{n}{n_{i}} = |\phi|e^{i(\beta - kr \cos \alpha)}$$
(14)

where γ_i is the incident free surface elevation. It is clear that the term $|\phi| e^{i(\beta-kr\cos\alpha)}$ is a factor which modifies the incident wave elevation to account for reflection and diffraction effects; thus, the amplitude of the normalized surface elevations may be expressed as the following wave amplitude factor:

$$\left|\frac{\eta}{\eta_{i}}\right| = \left|\phi\right| \tag{15}$$

The phase of Equation 14 is the following phase difference between incident and amplified waves:

Phase of
$$\frac{\eta}{\eta_{\mathbf{i}}} = \beta - kr \cos \alpha$$
 (16)

13. Output of the program PCDFRAC is comprised of $|\phi|$ and β . The amplification factor $|\phi|$ would then be multiplied by the incident wave height to obtain the actual wave height. The phase of the amplified wave β is a quantity not usually required in engineering practice; however, it may be useful on some occasions.

PART III: PCDFRAC OPERATIONAL DETAILS

Program Characteristics

14. The program PCDFRAC has been developed specifically for the problem of water wave diffraction and reflection from a vertical wedge of arbitrary wedge angle. It has been designed for operation on an IBM or IBM-compatible PC. A thin, rigid, impermeable semi-infinite breakwater is a special case in which the wedge angle is equal to zero. The program language is FORTRAN 77. The source code, PCDFRAC.FOR, requires 114 Kb of space, while the executable file, PCDFRAC.EXE, uses 74 Kb.

Input and Output

- 15. The program is divided into several parts. The first part is the main program PCDFRAC, with which the user works directly. It calls the solving subroutines and prints the answers in usable form. It also calculates wavelength from the input wave period by the Pade approximation to the linear dispersion relation (Chen and Thompson 1985). The subroutine PCWEDGES solves the actual problem and uses the mathematical subroutines BESJ, JAIRY, and GAMLN which are borrowed from the Naval Surface Weapons Center (NSCW) Library of Mathematics Subroutines (Morris 1984). Only the main program PCDFRAC and the <u>subroutine PCWEDGES</u> are listed in Appendix B. The main code of PCDFRAC is similar to that of WEDGE (See Chen 1987).
 - 16. Inputs into the program are as follows:
 - a. Constant water depth D, in feet.
 - b. Period T of the incident wave, in seconds.
 - <u>c</u>. Approach angle WAVEA of the incident wave, in degrees counter-clockwise from the positive X-axis.
 - <u>d</u>. Wedge angle WEDGEA of the obstacle, in degrees. A default of the program allows the semi-infinite breakwater case (WEDGEA = 0.0 deg) to be run.
 - \underline{e} . Location X,Y of the desired calculation, in feet from the tip of the wedge.

Figure 2 shows the preceding input conventions.

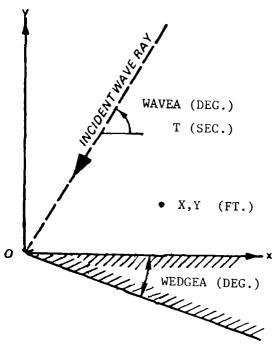


Figure 2. Input conventions for program PCDFRAC

- 17. The program outputs are:
 - a. Wavelength L, in feet.
 - <u>b</u>. Wave amplification factor $|\phi|$ as given in Equation 11, which is the ratio of wave height to incident wave height.
 - c. Wave phase β as given in Equation 12, in radians.
- 18. The program may be run either interactively (i.e., working directly with the user), or as a batch job (where the data is read from a file). These features will be discussed in further detail in Part V.
- 19. Equations 7 and 9 showed a summation of an infinite number of terms. This summation has been accommodated in the program by carrying the summation out to a term followed by eight successive terms in which the absolute value of the Bessel function is 10^{-8} or less. If the value of the solution is of the order of one, this corresponds to a truncation error of 10^{-8} or less.
- 20. For values of R/L (radial distance to point of calculation divided by wavelength) greater than 16, the statement "NO. OF TERMS FOR SUM-MATION IS INSUFFICIENT" may appear. This statement indicates that the number of terms in the summation is insufficient to ensure the 10^{-8} truncation error and that the NN value in the PARAMETER statement in the subroutine PCWEDGES needs to be greater than the present value of 200 if accuracy is to be

maintained. In this case, the user should change NN from 200 to a larger value.

21. A program of this length would require a certain amount of run time on a PC. Tables Al and A2 (located in Appendix A) give run times (in seconds) for various values of the truncation error and R/L ratio. The times indicated are the lengths of time the computer would require to process one set of (x,y) coordinates for one incident wave angle and one incident wave period (on the order of seconds). It follows that the greater the truncation error allowed, the less time the computer would need to process one set of coordinates. It also follows that the greater the R/L ratio, the longer the computer would take to finish processing one set of coordinates, as more terms in the summation are required to ensure proper accuracy. Table Al is a collection of run times using an IBM AT-class computer, while Table A2 is comprised of run times on an IBM XT computer.

Required Equipment

- 22. The source code PCDFRAC.FOR and the executable file CDFRAC.EXE are contained on a floppy diskette which may be obtained upon user request. Additionally, the following equipment is either required or recommended:
 - \underline{a} . An IBM or IBM-compatible personal computer with a hard disk and disk operating system (DOS).
 - <u>b.</u> A FORTRAN compiler (installed in the computer). Major differences between various brands of compilers are not expected; however, the compiler must accept the Fortran 77 language.
 - c. One 5-1/4 in. disk drive.
 - d. Printer (optional).
 - e. Text editor.

PART IV: START-UP PROCEDURES

Copying Program onto Hard Disk

- 23. As mentioned earlier in this report, an IBM or IBM-compatible personal computer with DOS is required to use this program. Although Microsoft DOS Version 2.10 was used for this copying procedure, major deviations among various brands of DOS are not expected. To perform this procedure the user must:
 - a. Insert the floppy disk into a particular disk drive, and switch the operating drive of the computer to the drive and directory containing the Fortran compiler. For Microsoft DOS this is done by typing

C: CD/FORTRAN

<CR>

if the Fortran compiler were located in drive C and in directory FORTRAN. (The symbol <CR> denotes carriage return.)

<u>b</u>. Copy the program PCDFRAC.FOR onto the hard disk. For Microsoft DOS Version 2.10 this is done by typing

COPY A: PCDFRAC.FOR

<CR>

if the disk were in drive A. Now the program PCDFRAC.FOR is copied onto the same disk and into the same directory as the FORTRAN compiler.

Compilation of Program

24. Compilation of a program translates the language in which the program is written (in this case, FORTRAN) into the internal machine language of the computer. The procedure here is that of the Ryan-McFarland Version 1.00 Fortran compiler; however, major discrepancies among various compilers are not expected. To compile the program, the user should type

PROFORT PCDFRAC/E

<CR>

and compilation will begin. With the Ryan-McFarland Version 1.00 compiler,

the /E option added to the end of the file name will list any syntactical errors as they occur. There should be no errors.

25. Compiling the program on an IBM XT or XT-compatible computer takes about 12 min, primarily because of the length of the program. On an IBM AT or AT-compatible personal computer, compilation requires just over 4 min. When the compilation process is complete, the following message:

Compilation Complete: 0 Errors, 0 Warnings

should appear on the screen. An object file, PCDFRAC.OBJ, has been created as a result.

Linkage of Program

26. Linkage of the program with any external subroutines is done next. This is a necessary step with all programs, regardless whether any external subroutines are specified within the program. Linkage is done by typing

LINK PCDFRAC

<CR>

The following will then print to the screen, one at a time (each to be answered with a carriage return):

RUN FILE [PCDFRAC.EXE] <CR>
LIST FILE [NUL.MAP] <CR>
LIBRARIES [.LIB] <CR>

The above options actually refer to specific options in the linking process. These options are not directly involved with PCDFRAC and are not required for program execution. Linkage takes about 30-40 sec, regardless of the type of computer. After linkage, the usual computer prompt will appear, and an executable file, PCDFRAC.EXE, will have been created.

Execution of Program

27. The executable file, PCDFRAC.EXE, actually runs the program. If the user wished to use PCDFRAC without any intent to modify it, this file would be used exclusively. Additionally, no FORTRAN compiler is required to use PCDFRAC.EXE. To perform any modifications, however, the file PCDFRAC.FOR would be needed. If the program were modified in any way, it would need to be recompiled and relinked after the changes were completed. To execute the program the user should type

PCDFRAC <CR>

and the program will begin running.

PART V: PROGRAM EXECUTION

28. The program will offer the option of either operating directly with the user (interactive operation) or of reading and processing the data directly from an existing file (batch operation).

Interactive Option

- 29. The interactive option is recommended for users with a small amount of data. It is sequenced as follows:
 - a. The program will first ask whether a written output is desired. If so, the user will input the file name to be used. The program contains a feature which will alert the user if the file name specified matches that of an existing file. If this occurs, the program will offer the user the option of either entering a new file name or of overwriting the existing file. (Note: Limited to a maximum of an eight-character string, the file name can have fewer characters. Some examples of eight-character strings include: FAST.DAT, DIFRACTI, and WAVES-10.)
 - <u>b</u>. The program will then ask if the input data are stored in a file. Because the interactive option is to be used here, the answer is "no".
 - c. The program will then ask if the user would require a particular value for the wedge angle or the semi-infinite breakwater case. If a value for the wedge angle is needed, it would be input (in degrees) during this step.
 - d. The program will then request the following:

Water depth, in feet.
Incident wave period, in seconds.
Incident wave angle, in degrees counter-clockwise from the positive x-axis.

- e. Next the program will ask for the number of points to be input on the present run.
- \underline{f} . It will then ask for the (x,y) coordinates (in feet) of the desired points of calculation, one at a time.
- g. After all the points have been entered, it will then give the information in tabular form, including the input information. If the output were also written to a file, the user would be reminded of the file name.

30. In the example problem shown in Figure 3, it is desired to calculate the wave amplification factors at the locations shown, with the obstacle being a semi-infinite breakwater (wedge angle = 0.00). The interactive run for the example in Figure 3 is shown in Figure 4 with user input underlined. The resulting output is then sent to both the screen and any output file specified. It appears in Figure 5.

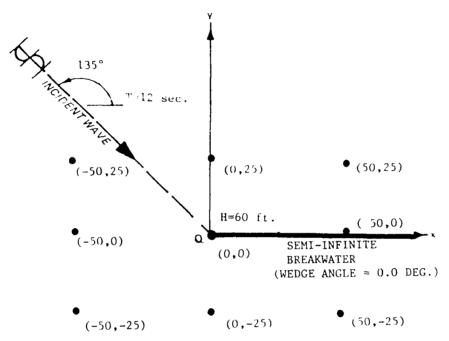


Figure 3. Example problem for semi-infinite breakwater

Explanation of Output

31. In the interactive output shown in Figure 5, the first three columns, as well as the fifth, sixth, and seventh columns, consist of user input which require no further explanation. The fourth column is the calculated wavelength. The last two columns comprise the primary solution, as given in Equations 11 and 12. AMP is the amplification factor for the incident wave. This number would be multiplied by the incident wave height to obtain the actual wave height at that particular (X,Y) location. PHA is the wave phase (in radians). This information is not usually required in most engineering applications but may be of use at times.

```
************************
* "PCDFRAC" - A PROGRAM WHICH CALCULATES WAVE AMPLIFICATION FACTORS
* BASED ON THE COMBINED DIFFRACTION AND REFLECTION OF WAVES BY A
* VERTICAL WEDGE OF ARBITRARY WEDGE ANGLE. THE PROGRAM ALSO CALCU- * LATES THE PHASE OF THE AMPLIFIED WAVE. THE PROGRAM WILL DEFAULT TO *
* ZERO WEDGE ANGLE (SEMI-INFINITE BREAKWATER CASE) IF NO WEDGE ANGLE *
* IS SPECIFIED.
***************
DO YOU WANT OUTPUT IN A FILE ? (0="NO", 1="YES") = 1
ENTER NAME OF OUTPUT FILE = TESTI.OP
IS INPUT DATA LOCATED IN A FILE ? (0="NO",1="YES") = 0
OPTION TO SET WEDGE ANGLE (DEFAULT VALUE = 0.00 DEG.)
SET WEDGE ANGLE ? (0="NO", 1="YES") = 0
SET INITIAL VALUES
INPUT WATER DEPTH (FT.) = 20
INPUT INCIDENT WAVE PERIOD (SEC.) = 8
INPUT INCIDENT WAVE ANGLE
(DEG. CCW FROM POSITIVE X - AXIS) = 135
HOW MANY POINTS DO YOU WISH TO ENTER (UP TO 99)? = 9
AT EACH PROMPT, DO THE FOLLOWING :
  1) TYPE IN X - COORDINATE
   a) TYPE A COMMA
   3) TYPE IN Y - COORDINATE
  4) FRESS "ENTER"
(X,Y) COORDINATES FOR FOINT NO. 1 (FT.) = -50.25
X.YN GOORDINATED FOR FOINT NO. 2 (FT.) = 0.25
(X,Y) COORDINATES FOR POINT NO. 3 (FT.) = 50.25
(X.Y) COORDINATES FOR POINT NO. 4 (FT.) \pm -50.0
(X,Y) COORDINATES FOR FOINT NO 5 (FT.) = 0.0
(X,Y) COORDINATES FOR POINT NO. 6 (FT.) = 50.0
(X,Y) COORDINATES FOR FOINT NO. (FT.) = -50.-25
(X,Y) COORDINATES FOR FOINT NO. 8 (FT.) = 0.-25
(X,Y) COORDINATES FOR POINT NO. 9 (FT.) = 50,-25
```

Figure 4. Interactive execution for problem in Figure 3

SEMI-INFI	NITE BRE	AKWATER (WI	EDGE ANG	LE = 0.0	O DEGRE	ES)		
DEPTH (FT)	PERIOD (SEC)	WAV.ANGLE (DEG)	WAVLNG.	WDG.ANG.	X (FT)	Y (FT)	AMP	PHA (RAD)
20.00	8.00	135.00	190.00	0.00	-50.00 0.00 50.00 -50.00 0.00 50.00 -50.00 0.00	25.00 25.00 25.00 0.00 0.00 -25.00 -25.00	0.98 1.04 1.44 1.00 1.00 1.69 1.03 0.86 0.60	1.77 0.45 -0.81 1.17 0.00 -0.90 0.59 -0.55 -2.18

YOUR OUTPUT IS IN TESTI.OP Execution terminated: 0

C>

Figure 5. Solution to problem in Figure 3

32. Figure 6 is an example problem in which the diffracting obstacle is a dock with a 90-deg wedge angle. It is desired to calculate the wave amplification factors at the locations shown. The interactive run and the output are both similar to those of the example shown in Figure 3 and require no

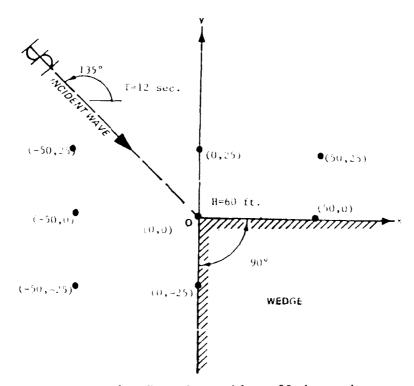


Figure 6. Example problem, 90-deg wedge

further explanation. The interactive run is shown in Figure 7, while the corresponding output is shown in Figure 8.

Batch Option

- 33. The batch operation is recommended for calculation of a large number of points or if the user requires calculations with several values of wave period, incident wave angle, and/or wedge angle. The batch operation is sequenced as follows:
 - <u>a.</u> The user will first create the file. An example appears in a following subsection. (Note: The file name must be kept to a maximum of eight characters, as before.)
 - b. The program will ask if a written output file is desired. If it is, the user will enter the name of the output file. As before, the program will alert the user if the chosen output file name matches that of an existing file. If so, the user will have the option of either overwriting the file, or enteranew file name.
 - c. It will then ask if the data are located in a file. Because batch operation is desired, the answer input by the user would be "yes".
 - \underline{d} . It will then request the input file name.
 - e. As it calculates, it will print the results to the screen in tabular form. If a written file was requested, it will write to the file in the same format.
 - \underline{f} . When completed, it will ask the user if any additional files need to be processed. If so, the user will input the name of the file.
 - g. The entire sequence is then repeated until there are no more input files left to process.
- 34. The input file for the batch job requires a specific format and can be created with any compatible text editor. The input file in Figure 9 contains data for the example problems in Figures 3 and 6. There is a limit of 300 values of X and Y which can be processed in one batch job. However, a greater number of values can be processed by changing the value of 300 in the DIMENSION statement in program PCDFRAC.FOR to a higher value. To create an input file, the following information is used:
 - a. Line 1 D,T,WAVFA,WEDGEA

The water depth, incident wave period, incident wave angle and wedge angle are input here. D appears in columns 1-10, T in columns 11-20, WAVEA in columns 21-30, and WEDGEA in

```
**************************
* "PCDFRAC" - A PROGRAM WHICH CALCULATES WAVE AMPLIFICATION FACTORS
* BASED ON THE COMBINED DIFFRACTION AND REFLECTION OF WAVES BY A
* VERTICAL WEDGE OF ARBITRARY WEDGE ANGLE. THE PROGRAM ALSO CALCU-
* LATES THE PHASE OF THE AMPLIFIED WAVE. THE PROGRAM WILL DEFAULT TO *
* ZERO WEDGE ANGLE SEMI-INFINITE BREAKWATER CASE) IF NO WEDGE ANGLE *
* IS SPECIFIED.
**************
DO YOU WANT OUTFUT IN A FILE ? (0="NO", 1="YES") = 1
ENTER NAME OF OUTPUT FILE = TESTI.OP
IS INPUT DATA LOCATED IN A FILE ? (0="NO",1="YES") = 0
OPTION TO SET WEDGE ANGLE (DEFAULT VALUE = 0.00 DEG.)
SET WEDGE ANGLE ? (0="NO",1="YES") = 1
ENTER WEDGE ANGLE (DEG.) = 90
SET INITIAL VALUES
INPUT WATER DEPTH (FT.) = 20
INPUT INCIDENT WAVE FERIOD (SEC.) = 8
INPUT INCIDENT WAVE ANGLE
(DEG. FOW FROM FOSITIVE X - AXIS) \approx 135
HOW MANY PRINTS IN YOU WISH TO ENTER (UP TO 99)? = 8
AT EACH PROMPT, DO THE FOLLOWING:
1) TYPE IN X - MOORDINATE
3) TYPE A COMMA
3) TYPE IN Y MOORDINATE
   4) FRESS ENTER
 X,Y) COORDINATED FOR FOINT NO. 1 (FT.) = -50.25
 X,Y COORDINATES FOR FOINT NO
                                2 (FT.) = 0.25
(X,Y) DORDINATES FOR FOINT NO. 3 (FT.) = 60.25
(X.Y. COORDINATES FOR FUINT NO.
                               4 (FT) = -50.0
(X,Y) -WORDINATES FUR POINT NO. (E. (FT.) = 0.0
 CONTRACTOR AND DESCRIPTION OF PT.
      JOURDINATES FOR FAINT NO. TO (FT.) = -60, (CF
(X,Y) DOORDINATES FOR FOINT NO. 3 (FT.) = 0, -25
```

Figure 7. Interactive execution for problem in Figure 6

OBSTACLE IS A VERTICAL WEDGE OF ANGLE 90.00 DEGREES FERIOD WAY, ANGLE WAYLNG, WDG, ANG. PHA (DEG) (RAD) 20.00 8.00 135.00 190.00 90.00 25.00 -50.00 0.90 0.00 25.00 1.01 0.30 25.00 50.00 1.43 - U.87 -50,00 0.00 0.75 1.18 0.00 0.00 0.00 1.33 50.00 0.00 1.71 -0.95-50.00 -25.00 0.75J.35 -25.00 0.00 1.53 -0.41

YOUR OUTPUT IS IN TESTI.OP Execution terminated: 0

C>

Figure 8. Solution to problem in Figure 6

20.00	8.00	135.00	90.00	
0.00	-25.00			
-50.00	-25.00			
50.00	0.00			
0.00	0.00			
-50.00	0.00			
50.00	25.00			
0.00	25.00			
50 .00	25.00			
20.00	8.00	135.00		
50.00	-25.00			
0.00	-25.00			
-50.00	-25.00			
50.00	0.00			
0.00	0.00			
-50.00	0.00			
50.00	25.00			
0.00	25.00			
-50.00	25.00			:

Figure 9. Sample input data file for Figures 3 and 6

columns 31-40. If the semi-infinite breakwater case is to be run, the input field for WEDGEA can be left blank.

b. Line 2 - X, Y, END

The location of the calculation is input on each line. X is input in columns 1-10, Y in columns 11-20, and END in column 50. END is an end-of-file marker alerting the computer that that particular line is the last line of X,Y data for the particular values of D, T, WAVEA, and WEDGEA. To denote the end of X,Y data, the user should enter 1 for END. Otherwise, the input field may be left blank. Successive sets of D, T, WAVEA, and WEDGEA data can then be entered, along with their corresponding sets of X,Y data.

35. The execution of the data file in Figure 9 is shown in Figure 10 with the user input underlined. Figure 11 shows the resultant output.

Figure 10. User input for execution of file in Figure 9

INPUT FIL	E = TEST	B.IP						
DEPTH (FT)	PERIOD (SEC)	WAV.ANGLE (DEG)	WAVLNG.	WDG.ANG (DEG)	. X (FT)	Y (FT)	AMP	PHA (RAD)
20.00	3.00	135.00	190.00	90.00	-			
					0.00	-25.00	1.53	-0.41
					-50.00	-25.00	0.75	0.35
					50.00	0.00	1.71	-0.95
					0.00	0.00	1.33	0.00
					-50.00	0.00	0.75	1.18
					50.00	25.00	1.43	-0.87
					0.00	25.00	1.01	0.30
20.00	8.00	135.00	190 00	0.00	-50.00	25.00	0.90	1.94
20.00	0.00	133.00	190.00	0.00	50.00	-25.00	0.60	-2.18
					0.00	-25.00	0.86	-0.55
					~50.00	-25.00	1.03	0.59
					50.00	0.00	1.69	-0.90
					0.00	0.00	1.00	0.00
					-50.00	0.00	1.00	1.17
					50.00	25.00	1.44	-0.81
					0.00	25.00	1.04	0.45
					-50.00	25.00	0.98	1.77
				_ ~				

YOUR OUTPUT IS IN TESTB.OP

DO YOU HAVE ANOTHER INPUT FILE ? (0="NO",1="YES") = 0

Execution terminated: 0

C>

Figure 11. Output for execution of sample input file in Figure 9

PART VI: SUMMARY

- 36. A brief theoretical outline of wave diffraction and reflection by a vertical wedge of arbitrary wedge angle has been presented. A personal computer code, PCDFRAC, which is a PC version of WEDGE (Chen 1987), has been implemented for calculating the wave amplification factors necessary to obtain wave heights in the near field of the vertical wedge due to diffraction and reflection.
- 37. The necessary procedures for setting up PCDFRAC on a personal computer have been documented in detail. Input and output files have also been described in detail. Possible applications of the program in field situations have been discussed and the execution of the program outlined in sequential order. Instructive examples of the execution of PCDFRAC have also been presented.

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APPENDIX A: RUN TIMETABLES

Table Al

Run Time* Versus Summation Truncation Error

IBM AT-Class

	T	runcation Error	
R/L Ratio	E-08	E-06	E-04
1.0	0.82	0.70	0.59
2.0	2.42	2.26	1.98
3.0	2.56	2.28	2.06
4.0	2.72	2.31	2.10
5.0	3.29	2.85	2.46
6.0	3.41	3.06	2.71
7.0	3.91	3.46	3.08
8.0	4.29	3.88	3.37
9.0	4.84	4.28	3.83
10.0	5.20	4.70	4.10
10.0	5.20	4.70	4

^{*} In seconds.

Table A2

Run Time* Versus Summation Truncation Error

IBM XT

	7	runcation Error	
R/L Ratio	E-08	E-06	E-04
1.0	2.15	1.65	1.49
2.0	4.20	4.11	3.03
3.0	4.85	4.76	4.29
4.0	5.65	5.08	4.32
5.0	5.85	5.10	4.38
6.0	6.04	5.65	4.50
7.0	7.04	6.04	5.50
8.0	7.25	6.60	5.97
9.0	8.14	6.87	6.10
10.0	8.95	7.66	7.17

^{*} In seconds.

APPENDIX B: PARTIAL LISTING OF PROGRAM PCDFRAC

```
PROGRAM PCDFRAC
      ******************
      *This program calculates wave amplification factors*
      *for the combined diffraction and reflection of
      *monochromatic incident waves of infinitesimal
      *amplitude coming from infinity by a vertical wedge*
      *of arbitrary wedge angle. It also calculates the
      *phase of the amplified wave. The program will
      *default to a zero wedge angle (semi-infinite
      *breakwater) if no wedge angle is specified.
      *******************
      Initialize and dimension variables
      REAL L, PI, PI2
      INTEGER END
      CHARACTER*8 OUTFILE
      CHARACTER*8 INFILE
      LOGICAL EXST
      DIMENSION X(300), Y(300), FABS(300), FPHA(300)
      PI=3.14159
      PI2=2.*PI
      WEDGEA=0.0
      ICOUNT = 0.0
      Program introduces itself
      WRITE (*,*)'
      PRINT 8001
     FORMAT(1X,70('*'))
      PRINT 8002
8002
     FORMAT (1X, '*', 68X, '*')
      PRINT 8003
     FORMAT (1X, '* "PCDFRAC" - A PROGRAM WHICH CALCULATES WAVE'
     1 ,1X, 'AMPLIFICATION FACTORS *')
      PRINT 8004
     FORMAT (1X, '* BASED ON THE COMBINED DIFFRACTION AND REFLECTION'
     1 ,1X, 'OF WAVES BY A
                              *')
     PRINT 8005
     FORMAT (1X, '* VERTICAL WEDGE OF ARBITRARY WEDGE ANGLE. THE'
     1 ,1X,'PROGRAM ALSO CALCU-
PRINT 8006
8006 FORMAT (1X, '* LATES THE PHASE OF THE AMPLIFIED WAVE. THE PROGRAM'
     1 ,1X,'WILL DEFAULT TO *')
      PRINT 8007
     FORMAT (1X,'* ZERO WEDGE ANGLE (SEMI-INFINITE BREAKWATER CASE)'
1 .1X,'IF NO WEDGE ANGLE *')
PRINT 8008
     FORMAT (1X,'* IS SPECIFIED.'.54X,'*')
     PRINT 8002
     PRINT 8001
     WRITE(*,*)
     Set option for writing output into file
```

```
991
       PRINT 2199
      FORMAT (36(' -'))
2199
       PRINT *, 'DO YOU WANT OUTPUT IN A FILE ? (0="NO", 1="YES") = '
       READ *, MM
       IF (MM .NE. 1 .AND. MM .NE. 0) GOTO 991
IF (MM .EQ. 0) GOTO 993
       PRINT 2199
      PRINT *, 'ENTER NAME OF OUTPUT FILE = '
READ (*, '(A)') INFILE
614
      INQUIRE (FILE=INFILE, EXIST=EXST)

IF (EXST .EQV. .TRUE.) THEN

PRINT *,'FILE ALREADY EXISTS; SELECT ONE OF THE FOLLOWING:'
613
       PRINT *.'
       PRINT 615
615
       FORMAT(1X, '0=ENTER ANOTHER FILE NAME ; 1=OVERWRITE OLD'
      1 ,1X,'FILE WITH NEW DATA')
       PRINT *.
       PRINT *, 'OPTION ? = '
       READ *, ANS
       IF (ANS .NE. 0 .AND. ANS .NE. 1) GOTO 613 IF (ANS .EQ. 1) THEN \,
       OPEN (2,FILE=INFILE,STATUS='UNKNOWN')
       ELSE
       GOTO 614
       END IF
       END IF
       OPEN (2, FILE=INFILE, STATUS='NEW')
       WRITE (2,2201) INFILE
      FORMAT (1X, 'OUTPUT OF PROGRAM "PCWEDGE" - FILENAME IS ', A8)
IF (ICOUNT .NE. 0.00) GOTO 998
2201
993
С
       Set Option for Interactive or Batch operation
Ċ
       PRINT 2199
       PRINT *, 'IS INPUT DATA LOCATED IN A FILE ? (0="NO",1="YES") = '
       READ *, NN
       IF (NN .NE. 0 .AND. NN .NE. 1) GOTO 993
       IF (NN .EQ. 0) GOTO 600
C
C
       Batch Operation Option
С
       PRINT*, 'ENTER NAME OF INPUT FILE = '
       READ (*,'(A)')OUTFILE
       OPEN (1,FILE=OUTFILE,STATUS= OLD )
       KCOUNT=0.00
998
       PRINT 2199
       WRITE (2,2199)
       PRINT 2143.OUTFILE WRITE (2.2143) OUTFILE
2143 FORMAT(1X, 'INPUT FILE = ', A8)
C
       Read the file - can have multiple values of h,t,wavea, and wedgea
С
       K = 1
```

```
1001
       READ (1,2100,END=999) D,T,WAVEA,WEDGEA
2100
       FORMAT(4F10.2)
        IF (D .LT. 0.00) THEN
       PRINT*, WATER DEPTH CANNOT BE NEGATIVE. EXECUTION STOPPED.' PRINT*, 'PLEASE CORRECT INPUT FILE AND RE - RUN.'
        GOTO 700
        ELSE
        END IF
        IF (T .LT. 0.00) THEN
       PRINT*, 'WAVE PERIOD CANNOT BE NEGATIVE. EXECUTION STOPPED.'
PRINT*, 'PLEASE CORRECT INPUT FILE AND RE - RUN.'
        GOTO 700
        ELSE
        END IF
       IF (WEDGEA .LT. 0.00 .OR. WEDGEA .GT. 180.00) THEN PRINT *,'WEDGE ANGLE MUST BE BETWEEN 0.0 AND 180.0 DEGREES.' PRINT *,'EXECUTION STOPPED.' PRINT *,'PLEASE CORRECT INPUT FILE AND RE - RUN.'
        GOTO 700
        ELSE
        END IF
        IF (KCOUNT .NE. 0.00) GO TO 6551
       WRITE (2,2199)
PRINT 2199
        PRINT 2049
        WRITE (2,2049)
2049
                                              ')
       FORMAT ('
        WRITE(2,2050)
        PRINT 2050
      FORMAT(3X,'DEPTH',3X,'PERIOD',2X,'WAV.ANGLE',1X,'WAVLNG.',
1 'WDG.ANG.',3X,'X',7X,'Y',5X,'AMP',4X,'PHA')
        WRITE(2,2051)
        PRINT 2051
2051 FORMAT(4X,'(FT)',4X,'(SEC)',4X,'(DEG)',4X,'(FT)',3X,'(DEG)',4X,
1 '(FT)',4X,'(FT)',9X,'(RAD)'/ 36(' -')/)
С
C
        Call subroutine PADES to calculate wavelength
C
6551
       CALL PADES(L,D,T)
        WRITE(2,2150) D,T,WAVEA,L,WEDGEA
2150
       FORMAT(F8.2.2X,F6.2,4X,F6.2,2X,F7.2,1X,F6.2)
        PRINT 2150, D, T, WAVEA, L, WEDGEA
        READ (1,2200,END=99) X(J),Y(J),END
98
2200
       FORMAT(2F10.2,25X,I5)
C
        Call subroutine MAIN to solve problem and deliver
Ċ
        solution
C
        CALL MAIN (F, FABS(J), FPHA(J), X(J), Y(J), L, WEDGEA, WAVEA)
        WRITE(2,2250) X(J), Y(J), FABS(J), FPHA(J)
       FORMAT(42X,2F8.2,2X,F4.2,2X,F5.2)
        PRINT 2250, X(J), Y(J), FABS(J), FPHA(J)
        X(J) = 0.00
        Y(J)=0.00
```

```
FABS(J)=0.00
      FPHA(J)=0.00
       IF (END .EQ. 1) GOTO 99
      J=J+1
      GOTO 98
99
      CONTINUE
      KCOUNT = KCOUNT + 1.00
      K=K+1
      GOTO 1001
999
      CONTINUE
      CLOSE(1,STATUS='KEEP')
      CLOSE(2,STATUS='KEEP')
PRINT *,'
      PRINT 2199
      IF (MM .EQ. 0) GOTO 994
      PRINT 222, INFILE
222
      FORMAT(1X, 'YOUR OUTPUT IS IN ', A8)
С
С
      Option to process additional input files
С
      PRINT *,
      PRINT *, 'DO YOU HAVE ANOTHER INPUT FILE ? (0="NO",1="YES") = '
994
      READ ★,II
      IF (II .NE. 1 .AND. II .NE. 0) GOTO 994
      IF (II .EQ. 0) GOTO 700
      PRINT *, 'ENTER NEW INPUT FILE NAME = 'READ (*,'(A)') OUTFILE
      OPEN (1, FILE=OUTFILE, STATUS='OLD')
      ICOUNT = ICOUNT+1.0
      GOTO 991
C
C
      Interactive option
С
600
      PRINT 2199
      PRINT *, 'OPTION TO SET WEDGE ANGLE (DEFAULT VALUE = 0.00 DEG.)'
      PRINT 2049
      PRINT *, SET WEDGE ANGLE ? (0="NO",1="YES") = '
15
      READ *, LOGIC
      IF (LOGIC .NE. 1 .AND. LOGIC .NE. 0) GOTO 15 IF (LOGIC .EQ. 1) THEN
702
      PRINT *, 'ENTER WEDGE ANGLE (DEG.) = '
      READ *, WEDGEA
      IF (WEDGEA .GT. 180.0 .OR. WEDGEA .LT. 0.00) THEN
      PRINT *,'WEDGE ANGLE MUST BE BETWEEN 0.0 AND 180.0 DEGREES.' PRINT 2049
      GOTO 702
      ELSE
      END IF
      ELSE
      WEDGEA = 0.0
      END IF
С
С
      Get the facts: Initial values input in this step
С
120
      PRINT 2199
```

```
PRINT *, 'SET INITIAL VALUES'
       PRINT 2049
602
       PRINT *, 'INPUT WATER DEPTH (FT.) = '
       READ *, D
       IF (D .LT. 0.00) THEN
       PRINT *, 'WATER DEPTH CANNOT BE NEGATIVE.'
       PRINT 2049
       GOTO 602
       ELSE
       END 1F
603
       PRINT *, 'INPUT INCIDENT WAVE PERIOD (SEC.) = '
       READ *, T
       IF (T .LT. 0.00) THEN
PRINT *,'INCIDENT WAVE PERIOD CANNOT BE NEGATIVE'
       PRINT 2049
       GOTO 603
       ELSE
       END IF
       PRINT *,'INPUT INCIDENT WAVE ANGLE'
PRINT *,'(DEG. CCW FROM POSITIVE X - AXIS) = '
701
       READ *, WAVEA
       PRINT 2199
       WRITE (2,2199)
С
C
       Call subroutine PADES to calculate wavelength
C
730
       CALL PADES(L,D,T)
       IF (WEDGEA .NE. 0.00) THEN
       WRITE (2,2001) WEDGEA
2001
      FORMAT (1X, 'OBSTACLE IS A VERTICAL WEDGE OF ANGLE ', F6.2
      1 , ' DEGREES')
       ELSE
       WRITE (2,2002)
2002
      FORMAT(1X, 'SEMI-INFINITE BREAKWATER (WEDGE ANGLE'
      1 ,1X,'= 0.00 DEGREES)')
       END IF
       PRINT 2049
       WRITE (2,2049)
       WRITE (2,2050)
       WRITE (2,2051)
       WRITE (2,2150) D,T,WAVEA,L,WEDGEA
710
       PRINT *, 'HOW MANY POINTS DO YOU WISH TO ENTER (UP TO 99)? =
       READ *, KK
       PRINT 667
     FORMAT(1X, 'AT EACH PROMPT, DO THE FOLLOWING:',/
1,4X,'1) TYPE IN X - COORDINATE',/,4X,'2) TYPE A COMMA'
2,/,4X,'3) TYPE IN Y - COORDINATE',/,4X,'4) PRESS "ENTER"',/)
667
       DO 10 I=1.KK
       PRINT 2000, 1
2000 FORMAT (1X, '(X,Y) COORDINATES FOR POINT NO. ',12 1 ,1X,' (FT.) = ')
      READ \star .X(I),Y(I)
C
      Call subroutine MAIN to solve problem and deliver
      solution
```

```
C
      CALL MAIN (F, FABS(1), FPHA(1), X(1), Y(1), L, WEDGEA, WAVEA)
      WRITE (0,2250) X(I),Y(I).FABS(I),FFHA(I)
10
      CONTINUE
      CLOSE(2,STATUS='KEEP')
      FRINT 2199
      IF (WEDGEA .NE. 0.00) THEN PRINT 2001, WEDGEA
       PRINT 2049
      ELSE
      PRINT 2002
PRINT 2049
      END IF
       PRINT 2050
      PRINT 2051
PRINT 2150, D, T, WAVEA, L, WEDGEA
      Screen Output
č
       DO 20 N=1,KK
PRINT 2250,X(N),Y(N),FABS(N),FFHA(N)
20
       CONTINUE
       PRINT +.
       IF (MM .EQ. 0) GOTO 700
       PRINT 222, INFILE
700
       STOF
       END
C
(:
       Subroutine PADES, to calculate wavelength .
C C
       Based on Pade's approximation solution for the linear
       dispersion relation
       CUBROTTINE PADES(L,D,T)
       REAL L
       PI:3.14159
       PI2-2.*PI
       UMGA=1:12/T
       OMGG = OMGA * *2.732.2
       A=OMGG*D
       BB-A*(A+1./(1.+A*(0.66667+A*(0.35550+A*(0.16084+A*(0.06320+A*
      1 (0.02174+A*(0.00654+A*(0.00171+A*(0.00039+A*0.00011)))))))))
       B=SQRT(BB)
       FK=B/D
       TEPTIBLEK
       RETURN
       END
       Subroutine MAIN, which normalizes the input and calls
       Satr atime WEDGES, which solves the actual problem.
       MUBROUTINE MAIN(F. FABS, FFHA. X, Y, L, WEDGEA, WAVEA)
       REAL 1.
PI-3.14159
       FID ...*FI
XX ABS(X/L)
```

```
YY=ABS(Y/L)
     XRL=SQRT((XX**2.0)+(YY**2.0))
     IF (X_i, E\tilde{Q}_i, (0.00)] AND, Y_i, LT_i, (0.00) THEN
     XTH=1.5*FI
     GOTO 351
     ELSE
     IF (X .EQ. 0.00 .AND. Y .GT. 0.00) THEN
     XTH = 0.5 * PI
     GOTO 351
     ELSE
     GOTO 428
     END IF
     END IF
428
     IF (XX .EQ. 0.00 .AND. YY .EQ. 0.00) THEN
     XTH = 0.00
     GOTO 351
     ELSE
     XTH=ATAN(YY/XX)
     END IF
     IF (X .LT. 0.00)GOTO 100
IF (Y .LT. 0.00) GOTO 300
     GOTO 400
100
     IF (Y .LT. 0.00) GOTO 200
     XTH=PI-XTH
     GOTO 400
200
     XTH=PI+XTH
     GOTO 400
300
     XTH=PI2-XTH
400
     IDX=0.0
351
     CALL FOWEDGES(F, FABS, FPHA, XRL, XTH, WEDGEA, WAVEA, IDX)
     RETURN
     END
     SUBROUTINE POWEDGES (F. FABS, FPHA, XRL, XTH, WEDGEA, WAVEA, IDX)
 * THIS COMPUTER PROGRAM WAS PREPARED UNDER THE EFFORT OF CIVIL WORK
  * R&D FROGRAM OF COE. NEITHER ANY OF AGENCIES NOR ANYONE ASSUMES
  * ANY JEGAL LIABILITY OR RESPONSIBILITY FOR THE ACCURACY OF THE
  * FROGRAM.
  WAVE SCATTERING BY A WEDGE OBSTACLE. NUMBER OF SUMMATION TERMS 13
  NN. IDX=0 TO CALL BESJ.
     FARAMETER WN=100
     DIMENSION BJ(NN), W(NN), XM(NN)
     COMPLEX F.TM
     DATA TOLR/1.E-8/, ITER/8/
IF (IDX NE. 0) GOTO 4
     DO : 1-1.4N
     EJ(I) - C.OO
     :1-3.141592654
     CPI=FI/180.
     XKR:XRL*2.J*PI
     TH-XTH
```

```
WA=WAVEA*CFI
    XNU=(360.-WEDGEA)/180.
   RM(1) = 1.0
   IF(IDX.NE.O) GOTO 14
   CALL BESJ(XKR.O.O,1,W,NZ)
   \mathrm{BJ}\left( \left| 1\right\rangle \right\rangle =W\left( \left| 1\right\rangle \right\rangle
    ICOUNT=0
   DO 10 N=1,NN
   N1 = N + 1
   ICOUNT = ICOUNT + 1
   IF(ICOUNT.LE.ITER) GOTO 8
   NNN=N
   GOTO 14
 8 XM(N1)=FLOAT(N)/XNU
   M=INT(XM(N1))
   ALPHA=XM(N1)=M
   M1 = M + 1
   CALL BESJ(XKR, ALPHA, M1, W, NZ)
   IF(N1.EQ.NN) WRITE(6,9) XKR, ALPHA, M1, W(M1), NZ
 9 FORMAT(/' **** NO. OF TERMS FOR SUMMATION IS INSUFFICIENT ****'.
  1 /' XKR, ALPHA, M1, W(M1), NZ = ', 2F10.4, I5, E15.6, IE/)
   BJ(N1) = W(M1)
   IF(ABS(BJ(N1)).GT.TOLR) ICOUNT=0
10 CONTINUE
14 CONTINUE
   F \stackrel{\cdot}{=} BJ (1) \neq 2.
   DO 20 N=1,NNN
   N1 = N+1
   XMN=XM(N1)
   TM = (0.0, 1.0) * *XMN*BJ(N1) *COS(XMN*WA) *COS(XMN*TH)
   F = F + TM
CONTINUE
   F:4 XNU*F
   Fh-hEAL(F)
   FI=AIMAG(F)
   FABS=CGRT(FR*FR+FI*FI)
   IF(WALLE, 1, E-8) FABS = FABS/2.
    IF(FABS.LT.TOLR) GOTO 30
   FPHA-ATAN2(F1.FR)
   FETUEN
30 FEHA=0 0
   RETURN
    THE TIME (ESSITY, ALPHA, N.Y. NZ)
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APPENDIX C: NOTATION

Ao	-iga _ω /ω
a o	Incident wave amplitude
e	2.71828; base for natural logarithm
g	Gravitational acceleration
ħ	Water depth
i	$\sqrt{-1}$
Jo	Zeroth order Bessel function of the first kind
J _{n/v}	$\frac{\eta}{\nu}$ order Bessel function of the first kind
k	Wave number
(r,θ,z)	Cylindrical coordinate system
r	Radial coordinate
u	Flow velocity
z	Vertical coordinate
α	Approach angle of incident wave train
β	Phase of $\phi(r,\theta)$
η	Water surface elevation
n	Incident water surface elevation
$\dot{\theta}$	Angular coordinate
θ	Angular coordinate for water domain
v	$\theta_{o}/2\pi$
গ	3.14159
$\Phi(r,\theta,z,t)$	Three-dimensional, time-dependent velocity potential
¢(r,θ)	Velocity potential in horizontal plane
w	Radian frequency
Subscripts:	
r	Denotes r-coordinate variable
е	Denotes θ -coordinate variable
Mathematical	symbols:
9	Partial differentiation
Σ	Summation
11	Absolute value
Im()	Imaginary part
Re()	Real part